# Symmetry Guidelines for the Design of Convergent Syntheses. On Narcissistic Coupling and La Coupe du Roi 

Santiago Alvarez* and Félix Serratosa*<br>Contribution from the Departament de Química Inorgànica and Departament de Quimica Orgànica, Universitat de Barcelona, 08028 Barcelona, Spain. Received February 21, 1991


#### Abstract

A symmetry point group study of different segmentation patterns for molecules is presented as an aid for their retrosynthetic analysis. Symmetry properties of the target molecule allow the design of synthetic routes using either achiral, homochiral, or heterochiral isometric segments. It is found that chiral molecules can only be dissected into homochiral segments, whereas achiral molecules can only be fragmented into achiral or heterochiral segments in most cases. The only achiral molecules which can be dissected into homochiral segments (la coupe du roi) are those belonging to the $C_{n v}$ or $D_{n d}$ point groups, in two particular dissection modes.


## Introduction

The design of a chemical synthesis is based on a retrosynthetic analysis ${ }^{1}$ in which the target molecule is conceptually dissected into smaller fragments or synthons through the disconnection of bonds. High-symmetry molecules can sometimes be conveniently synthesized by joining together isometric segments ${ }^{1,2}$ through a convergent synthesis. ${ }^{4}$ In this case, the segments may be identical (achiral or homochiral segments) or enantiomeric pairs (heterochiral segments).

The convergent synthesis from homochiral segments and its reciprocal process, the bisection of an achiral molecule into homochiral fragments, are usually referred to as la coupe du roi. ${ }^{3}$ A recent example of the bisection of a molecule in a la coupe du roi mode has been reported by Cinquini et al. for cis-3,7-di-methyl-1,5-cyclooctanedione. ${ }^{5}$ On the other hand, the coupling of heterochiral segments to produce an achiral molecule has been named narcissistic coupling. ${ }^{6}$ This strategy has two major advantages: it is convergent and reflexive, ${ }^{7}$ and it does not require the resolution of the starting materials into optically pure enantiomers. Such a strategy has been proposed by Serratosa and co-workers ${ }^{8}$ for the synthesis of dodecahedrane.

Once the target molecule has been submitted to retrosynthetic analysis, the different ways in which some of the bonds may be disconnected must be evaluated. A symmetry point group ${ }^{9}$ study should allow us to establish some rules to determine which bond disconnections might lead to achiral, homochiral, or heterochiral segments. The aim of this study is to analyze the different possible disconnections of a molecule into isometric segments according to its symmetry and the relationship between the resulting segments for each case. In what follows, we will consider bond disconnections (or bond cutting) as if they were always homolytic. Therefore, a heterolytic bond disconnection between two sym-metry-related atoms may be conceptually considered in two

[^0]successive steps: some asymmetry ("functionalization") is first introduced into the bond, which is then cut ("disconnection"). Alternatively, the bond is first cut ("disconnection"), and alternate positive and negative charges (indicating the electrophilic and nucleophilic character of the atoms) are assigned to the "disconnected" atoms (in the resulting fragments), which are then properly "functionalized" in order to attain the formal charges assigned. Both approaches are summarized in 1.



$\mathbf{S}_{6}$


1

Although the methodologies and strategies discussed here have been developed mainly in the area of organic chemistry, the formation of transition metal coordination compounds can be also considered in a similar way. Multinuclear transition metal compounds with either metal-metal bonded skeletons or bridging ligands can also be imagined to be formed by isometric fragments which could eventually undergo self-assembly reactions.

In a slightly different approach, coordination compounds can be considered as supermolecules in which the metal ion(s) hold the ligands together. Ligand dissociation can then be considered, within the framework of this paper, as the fragmentation of the complex into isometric segments (the ligands), disregarding the presence of the metal ion(s). An example of such an approach is given by the case of the double helicates synthesized by Lehn and co-workers. ${ }^{10}$ Moreover, the bond connection-disconnection terminology and the analysis of the relationships between segments

[^1]could also be applied in template syntheses, ${ }^{11}$ since the presence of a transition metal ion at the center of symmetry of the molecule does not affect the symmetry of the ligand array (typically a macrocyclic system).

Mislow and co-workers ${ }^{3}$ have recently examined the problem of dividing finite geometric objects into isometric segments, including the special case of la coupe du roi. Our systematic analysis based on symmetry point groups corroborates some of the statements made by these authors and establishes more general rules and some new conclusions.

## Symmetry Relationships between a Molecule and Its Segments

In order to study how the symmetry of a molecule dictates the ways in which it can be isometrically segmented and to define the relative chirality of the resulting segments, the following premises must be first stated.
(1) The molecule belongs to a symmetry point group $\mathbf{G}$. When several conformers are possible around the bond to be cut, the highest symmetry conformer will be considered.
(2) If the molecule can be fragmented into isometric segments, these are necessarily related by a symmetry operation $\mathbf{R}, \mathbf{R}$ being an element of $\mathbf{G}$.
(3) In the general case, the molecule can be fragmented in several different ways, depending on the symmetry operation chosen to define the isometric segments. For each fragmentation pattern, the number of segments produced is thus determined by symmetry.
(4) In order to generate isometric segments, a complete set of bonds related through one of the symmetry operations of $\mathbf{G}$ must be cut. Notice that in polycyclic molecules it may be necessary to cut more than one set of bonds in order to obtain independent segments. Notice also that a complete set of bonds is not necessarily formed by the $n$ bonds related through $C_{n}$, for example, since there are only $n / m$ bonds related through $C_{n / m}$.
(5) The symmetry operation which relates the isometric segments of a molecule is not a symmetry operation of the segments. As a result, the point group of a segment, $\mathbf{S}$, is a subgroup of $\mathbf{G}$. All of the symmetry operations in $\mathbf{G}$ can be obtained by successive application of the powers of $\mathbf{R}$ and the symmetry operations in $\mathbf{S}$, i.e., $\mathbf{G}=\mathbf{S} \times \mathbf{R} .^{12}$ It is obvious that all of the isometric segments belong to the same symmetry group $S$. The special case of molecules of low symmetry with fragments of higher local symmetry, in which $\mathbf{S}$ might not be a subgroup of $\mathbf{G}$, will not be considered in this paper.
(6) If the isometric segments are related by a proper rotation, $C_{n}$, they are superimposable (i.e., they may be either achiral or homochiral, but never heterochiral).
(7) Chiral segments related in the molecule through an $S_{n}$ operation (including reflections, $S_{1}$, and inversion, $S_{2}$ ) are enantiomers (heterochiral segments).
(8) When a molecule has at least one atom sitting on a symmetry element, nonisometric segments are also necessarily obtained. This is the case of mononuclear coordination compounds, in which dissociation reactions would produce several isometric segments (ligands) plus the central atom.

## Dissection Patterns and Molecular Symmetry

When a molecule is fragmented into isometric segments, the symmetry operation which converts the segments into each other is lost. For the subsequent discussion it is important to know the relationships between the particular dissection pattern applied to
(11) For accounts on template syntheses, see: (a) Melson, G. A., Ed. Coordination Chemistry of Macrocyclic Compounds; Plenum: New York, 1979. (b) Black, D. St. C. In Comprehensive Coordinalion Chemistry; Wilkinson, G., Gillard, R. D., McCleverty, J. A., Eds.; Pergamon Press: Oxford, 1987; Vol. 6, p 155. (c) Healy, M. de S.; Rest, A. J. Adv. Inorg. Chem. Radiochem. 1978, 21, 1. (d) Gerbeleu, N. V.; Zhovmir, F. K. Russ. J. Inorg. Chem. 1982, 27, 309. (e) Mertes, K. B.; Lehn, J.-M. In Comprehensive Coordination Chemistry; Wilkinson, G., Gillard, R. D., McCleverty, J. A., Eds.; Pergamon Press: Oxford, 1987; Vol. 2, p 915. (f) Vogel, E.; et al. Angew. Chem., Int. Ed. Engl. 1988, 27, 406, 409, 411.
(12) For an account of the relationships between symmetry operations in a symmetry point group, see: Hall, L. H. Group Theory and Symmetry in Chemistry; McGraw-Hill: New York, 1969.

Table I. Effect of Different Dissection Patterns on the Existing Symmetry Operations

| dissection <br> pattern | operations <br> preserved | operations <br> destroyed | operation <br> relating <br> segments |
| :--- | :--- | :--- | :--- |
| $\sigma / \sigma$ | $\sigma^{\perp}, C_{n}{ }^{\perp}$ | $\sigma^{\\|}, C_{n}{ }^{1}, S_{n} \perp, S_{n}{ }^{\\|}, \mathrm{i}$ | $\sigma$ |
| $S_{n} / \sigma$ | $C_{n / 2}(n$ even $), \sigma^{\perp}$ | $C_{n}, S_{n}{ }^{\perp}, S_{n}{ }^{\perp}, \sigma^{\perp}$ | $\sigma$ |
| $C_{n} / \sigma_{v}$ | $\sigma_{v}(n$ odd $), \sigma_{h}, C_{2} \perp$ | $C_{n}, S_{n} \perp$ | $C_{n}$ |
|  | $\sigma_{d}(n$ even $), \sigma_{h}, C_{2} \perp$ | $C_{n}, \sigma_{v}, S_{n}{ }^{\perp}$ | $C_{n}$ |
| $C_{2} / C_{n}$ | $C_{n}{ }^{\perp}$ | $C_{2}$ |  |
| $C_{n} / \mathrm{g}$ | $\sigma_{h}$ | $C_{n}, \sigma_{v}, \sigma_{d}$ | $C_{n}$ |
| $S_{n} / \mathrm{gc}$ | $C_{n / 2}(n$ even $)$ | $S_{n}, \sigma_{h}$ | $\sigma$ |
| $S_{n} / \mathrm{g}$ | none | i | $\sigma$ |
| $\mathrm{i} / \mathrm{i}$ |  | i | $\sigma$ |
| $\mathrm{i} / \mathrm{g}$ |  |  | $\sigma$ |

the molecule, the symmetry elements that are lost or retained by the segments, and those which remain in each segment. Let us identify each dissection pattern by a symbol of the type $\mathbf{R} / \mathbf{p}$, where $\mathbf{R}$ is the symmetry operation which relates the resulting segments and $\mathbf{p}$ refers to the position of the disconnected bonds relative to the symmetry elements of the molecule. The parameter $p$ can be either $\sigma$ for a bond passing across a symmetry plane (or a pseudosymmetry plane; see below), $C_{n}$ for a bond across a proper rotation axis but not across a symmetry plane, or $g$ for a bond in a general position and not passing through a symmetry plane or a proper rotation axis. Other types of positions $\mathbf{p}$ will be introduced later.

We start by looking at those bond disconnections which split the molecule into two halves. In other words, we cut all of the bonds that go across a reference plane. Any molecule can be idealized as a sphere with some symmetry elements, and its stereographic projection may be represented as in 2 . Even if the

cutting plane is a symmetry plane of the molecule, it is not a symmetry plane of each fragment, i.e., that plane is lost upon cutting. All symmetry elements not perpendicular to the cutting plane ( $C_{m}, C_{k}$, and $\sigma^{\prime \prime}$ in 2 ) exchange pieces of both fragments, i.e., the associated symmetry operations are lost upon fragmentation. What symmetry elements are retained by the fragments? Only the mirror planes and proper rotation axes perpendicular to the cutting plane are retained ( $C_{n}, \sigma^{\prime}$, and the plane of the paper). If a perpendicular improper rotation axis is present (e.g., $S_{n}$ in 2 ), it is also lost upon cutting since its reflection component converts pieces of both fragments into each other.

Now, not every plane can be used as a cutting plane. The two fragments are required to be isometric, so they must be related by a symmetry operation. We consider two possible cases: in one, the cutting plane is a symmetry plane, the resulting segments are mirror images of each other, and the dissection pattern will be abbreviated $\sigma / \sigma$ in the following. In the second case, the cutting plane is the reflection component of an improper rotation (not necessarily a symmetry plane, but we can consider it as a pseudosymmetry plane), and the dissection strategy should be abbreviated $S_{n} / \sigma$, indicating that the resulting fragments are related in the molecule by the improper rotation $S_{n}$ and that the disconnected bonds cross a pseudosymmetry plane. It is enough to rotate one of the disconnected segments by an angle of $2 \pi / n$ to find that it is the mirror image of the other one (i.e., if the segments are disymmetric, they must be heterochiral). The only difference between the $\sigma / \sigma$ and $S_{n} / \sigma$ cases is that the existence of a pseudosymmetry plane implies a perpendicular improper axis $S_{n}$. We have already stated that improper rotations are lost when cutting through a plane; a proper rotation $C_{n / 2}$ colinear with $S_{n}$ must exist
for even $n$ and a colinear $C_{n}$ for odd $n$. Since these proper rotation axes are perpendicular to the cutting plane, they are retained by the fragments. All of this is summarized in Table I.

A different strategy consists of splitting the molecules into two or more fragments related by a proper rotation $C_{n}$. Let us first study those cases in which there are $n$ symmetry planes containing the rotation axis ( $\sigma_{v}, \sigma_{v}{ }^{\prime}, \sigma_{v}{ }^{\prime \prime}$, and $\sigma_{d}$ in 3). Bonds can then be disconnected across equivalent symmetry planes, i.e., separated by angles of $2 \pi / n$, as shown in 3 . This strategy is therefore called


3
$C_{n} / \sigma$. For odd $n$, each segment retains one of the $\sigma_{v}$ planes. For even $n$, the $\sigma_{v}$ planes are lost, but there are always $\sigma_{d}$ planes which are retained by the segments. The proper rotation $C_{n}$ interconverts the segments, but it is not a symmetry operation of each segment. If there are binary rotation axes at the intersection of the remaining planes and the plane of the paper, they continue to be symmetry operations of the segments. All other rotations are lost upon segmentation. If a $\sigma_{h}$ symmetry plane exists in the molecule, each segment will keep such a symmetry plane. Notice that the existence of $\sigma_{h}$ together with $\sigma_{v}$ implies the existence of $C_{2}$ and, conversely, the existence of $\sigma_{v}$ and $C_{2}$ implies the existence of $\sigma_{h}$. A brief summary of the results for the $C_{n} / \sigma$ strategy is presented in Table I.

If the bonds to be cut are not across a symmetry plane but across a $C_{2}$ axis, as represented by the stereographic projection 4, a perpendicular axis $C_{n}$ (if present) is retained in each fragment, but other symmetry elements disappear. In the absence of a symmetry plane, the two isometric segments are related through a $C_{2}$ rotation. Hence, these are $C_{2} / C_{n}$ dissection patterns.


4
One can also choose to disconnect bonds that are related by a proper rotation $C_{n}$ but do not cross symmetry planes or axes, which may not even be present in a particular molecule. This is a $\boldsymbol{C}_{n} / \mathbf{g}$ dissection pattern. We can now use the stereographic projection 5 and cut the bonds at the positions indicated by the arrows. It is clear that $C_{n}$ and the symmetry planes $\sigma_{v}$ and $\sigma_{d}$ are lost. Other rotation axes are also lost. Only a $\sigma_{h}$ plane, if present, remains as a symmetry element of each segment.


5
If we disconnect bonds related by an improper rotation $S_{n}$, but not by a perpendicular symmetry plane nor by the coaxial proper
rotation of the same order, the improper rotation and any perpendicular symmetry planes are lost. A $C_{n / 2}$ rotation can be preserved, depending on the connectivity of the molecule. In 6 , the two shaded pieces (above the plane of the paper) remain connected after dissection, retaining a $C_{n / 2}$ rotation, and the same applies for the two white pieces (below the plane of the paper).


This will be referred to as an $S_{n} /$ ge dissection, the c referring to the fact that some connectivity between the smallest possible isometric segments remains after dissection. This is what happens if there are two atoms or two bonds sitting on the improper rotation axis. If there are no additional bonds connecting such pieces (the $S_{n} / \mathbf{g}$ pattern), isometric segments result with no symmetry element. Notice that $S_{n} / \mathbf{g}$ is equivalent to the successive application of $S_{n} / \mathrm{gc}$ and $C_{n / 2} / C_{n / 2}$. Other types of $S_{n} / \mathrm{p}$ dissection patterns will be discussed later during the analysis of the $D_{n d}$ point groups.

When a bond located at a center of inversion is cut and the molecule is split into two segments related only through the inversion, this symmetry operation is lost and the resulting segments are mirror images of each other. This dissection pattern is naturally called $\mathrm{i} / \mathrm{i}$. Similarly, if two bonds related only through inversion are cut, in an $\mathrm{i} / \mathrm{g}$ dissection pattern, two mirror-related segments result with no inversion center.

Finally, two geometric restrictions apply to bond cutting: If one or more atoms are sitting on a symmetry element $\mathbf{Q}$, neither the $\mathbf{Q} / \mathbf{p}$ nor the $\mathbf{R} / \mathbf{Q}$ dissection is allowed (i.e., they would not produce isometric segments). The above analysis of the relationships between bond disconnections and symmetry operations retained by the segments provides us with most of the information needed to decide which cutting strategy can split a molecule of known symmetry into either achiral, homochiral, or heterochiral segments. In general, for each possible dissection pattern in a particular point group G, we can easily identify, from Table I, which symmetry operations are lost and find the point group of the segments, $\mathbf{S}$. Also, the dissection pattern chosen determines whether the segments generated are related through a rotation (i.e., superimposable) or mirror images (see Table I). In the following, a systematic study of the results of the above dissection patterns for each family of point groups is presented, together with some examples of applications to real molecules.

## Segmentation of Chiral Molecules: $C_{n}$ and $D_{n}$ Groups

The only symmetry operations available in a chiral molecule are the proper rotations $C_{n}$, and consequently they can only belong to point groups $D_{n}$ or $C_{n}$ (disymmetric molecules) or to $C_{1}$ (asymmetric molecules). Since no isometric segments can be generated from an asymmetric molecule, we do not consider the $C_{1}$ point group here (see below). All of the subgroups of the $C_{n}$ and $D_{n}$ point groups are also of the $C_{n}$ or $D_{n}$ types; hence all isometric segments of $C_{n}$ or $D_{n}$ molecules are necessarily chiral (premise 5). Furthermore, all isometric segments of $C_{n}$ or $D_{n}$ molecules must be related by a proper rotation and are therefore homochiral, according to premise 6. A detailed summary of the results for $C_{n}$ molecules is presented in Table II.

Molecules belonging to a $D_{n}$ group can be fragmented in different ways: either into $n$ segments related by the $C_{n}$ rotation ( $C_{n} / \mathbf{p}$ dissections) or into two segments related by $C_{2}\left(C_{2} / \mathbf{p}\right.$ dissections). In the first case, depending on the position of the

Table II. Summary of the Different Patterns for Dissection of a Molecule into Isometric Segments ${ }^{a}$

| G | dissection pattern | number of segments | S | chirality of segments | examples ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $C_{1}$ | no | 1 |  |  |  |
| $C_{i}$ | i/g | 2 | $C_{1}$ | hetero |  |
| $C_{n}$ | $C_{n} / \mathrm{g}$ | $n$ | $C_{1}$ | homo | S |
| $D_{n}$ | $C_{n} / C_{2}$ | $n$ | $C_{2}$ | homo |  |
|  | $C_{n} / \mathbf{g}$ | $n$ | $\mathrm{C}_{1}$ | homo | s |
|  | $C_{2} / \mathrm{g}$ | 2 | $C_{1}$ | homo |  |
|  | $C_{2} / C_{n}$ ( $n$ even) | 2 | $C_{2}$ | homo |  |
|  | $C_{2} / C_{n}(\underline{ }$ odd) | 2 | $C_{1}$ | homo |  |
| $C_{s}$ | $\sigma / \sigma$ | 2 | $C_{1}$ | hetero |  |
| $C_{n v}$ | $\sigma_{v} / \sigma_{v}$ ( $n$ even) | 2 | $C_{s}$ | achiral | s |
|  | $\sigma_{v} / \sigma_{v}(\underline{\text { odd }}$ ) | 2 | $C_{1}$ | hetero | s |
|  | $C_{n} / \mathrm{g}$ | $n$ | $C_{1}$ | homo | s |
|  | $C_{n} / \sigma_{v}$ | $n$ | $C_{s}$ | achiral | $s$ |
|  | $2 C_{n} / \sigma_{v}$ | $2 n$ | $C_{1}$ | pairwise hetero | s |
| $C_{n h}$ | $\sigma_{h} / \sigma_{h}$ | 2 | $C_{n}$ | hetero | Figure 3 |
|  | $C_{n} / \mathrm{g}$ | $n$ | $C_{5}$ | achiral | s |
|  | $\mathrm{C}_{2} / \mathrm{C}_{2}$ | 2 | $C_{3}$ | achiral | Figure 3 and s |
|  | $S_{n} / \mathbf{g c}$ | 2 | $C_{n / 2}$ | hetero |  |
|  | $S_{n} / \mathbf{g}$ | $n$ | $C_{1}$ | pairwise hetero |  |
| $S_{n}$ | $S_{n} / \mathrm{gc}$ | 2 | $C_{n / 2}$ | hetero | Figure 4 and s |
|  | $S_{n} / \mathrm{g}$ | $n$ | $C_{1}$ | pairwise hetero | Figure 4 and s |
| $D_{n d}$ | $\sigma_{d} / \sigma_{d}$ ( $n$ even) | 2 | $C_{5}$ | achiral |  |
|  | $\sigma_{d} / \sigma_{d}(n$ odd $)$ | 2 | $C_{2}$ | hetero |  |
|  | $C_{n} / C_{2}$ | $n$ | $\mathrm{C}_{2}$ | homo | s |
|  | $C_{n} / \mathrm{g}$ | $n$ | $C_{1}$ | homo | s |
|  | $S_{2 n} / \sigma_{d} \mathbf{c}$ | 2 | $D_{n}$ | hetero |  |
|  | $S_{2 n} / \sigma_{d}$ | $2 n$ | $C_{2}$ | pairwise hetero |  |
|  | $S_{2 n} / C_{2} \mathrm{c}$ | 2 | $C_{n v}$ | achiral | $s$ |
|  | $S_{2 n} / C_{2}$ | $2 n$ | $C_{s}$ | achiral | s |
|  | $S_{2 n} / \mathrm{gc}$ | 2 | $C_{n}$ | hetero | 10 |
|  | $S_{2 n} / \mathrm{g}$ | $2 n$ | $C_{1}$ | pairwise hetero | 10 and $s$ |
|  | $C_{2} / C_{2}$ | 2 | $C_{s}$ | achiral | $s$ |
| $D_{n h}$ | $\sigma_{v} / \sigma_{v}(n$ even) | 2 | $C_{2 v}$ | achiral | s |
|  | $\sigma_{v} / \sigma_{v}(n$ odd $)$ | 2 | $\mathrm{C}_{s}$ | achiral | s |
|  | $\sigma_{h} / \sigma_{h}$ | 2 | $C_{n v}$ | achiral | s |
|  | $C_{n} / \sigma_{v}$ | $n$ | $C_{2 v}$ | achiral | s |
|  | $C_{n} / \mathrm{g}$ $S_{n} / \mathrm{gc}$ | $n$ | ${ }_{C}$ | achiral | s |
|  | $S_{n} / \mathrm{gc}$ | $n$ | $C_{s}$ | achiral |  |

${ }^{a} \mathrm{G}$ and S are the symmetry point groups of the molecule and the segments, respectively. ${ }^{b} \mathrm{Ans}$ in this column indicates that an example is provided as supplementary material.
disconnected bonds relative to the $C_{2}$ axis, the segments will be either asymmetric ( $C_{1}$ point group) or disymmetric ( $C_{2}$ point group). Similar results are found for the $C_{2} / \mathbf{p}$ dissection patterns (Table II).
A good example of fragmentation of disymmetric molecules is provided by the double-stranded helicates reported by Lehn et al. ${ }^{10}$ (Figure 1). These compounds belong to the $D_{2}$ point group for any length of the double helix. Consequently, the only conceivable fragmentation mode for the double-stranded helicates yields only two homochiral segments (ligands).

According to statement 2 above, asymmetric molecules cannot be fragmented into isometric segments. However, molecules such as $(1 R, 2 R)$-1,2-dichloro-1,2-dibromoethane or ( $1 R, 2 S$ )-1,2-di-chloro- 1,2 -dibromoethane, which are asymmetric in the general conformation, must be analyzed in their most symmetric conformation according to statement 1 . Thus, these molecules should not be considered as asymmetric but rather as belonging to the $C_{2}$ and $C_{s}$ point groups, respectively, and both can be split into two isometric segments.

## Segmentation of Achiral Molecules

Achiral molecules possess at least one improper rotation $S_{n}$, considering reflections and inversion as $S_{1}$ and $S_{2}$, respectively. They belong to any symmetry group other than $C_{1}, D_{n}$, or $C_{n}$. Fragmentation of such molecules can yield either chiral or achiral segments, depending on the fragmentation pattern chosen. We will focus mainly on the generation of chiral segments in the following section.

When the fragmentation pattern is such that isometric chiral segments are related through a $C_{n}$ rotation, these are homochiral. Notice the fragmentation of an achiral molecule into segments



Figure 1. Schematic representation of di- (a) and trinuclear (b) helicates belonging to the $D_{2}$ point group. The two sets of ligands are related through $C_{2}$, and each retains $C_{2}^{\prime}$ as a symmetry operation.
related by a proper rotation is not a sufficient condition for the segments to be chiral, since for many symmetry groups other symmetry operations must be simultaneously destroyed. If the segments are related through a reflection, an inversion, or an improper rotation, they will be heterochiral, according to premise 7. These segments can be further fragmented into smaller homochiral segments according to what is described in the preceding section, resulting in $n$ segments of each chirality. It is clear that the appropriate choice of the fragmentation pattern would allow the dissection an achiral molecule into either homo- or heterochiral segments. Whether both kinds of fragmentation or only one of them is possible depends on the symmetry group of the molecule and will be analyzed below.

A molecule belonging to the point group $C_{s}$ can only be cut into isometric segments along its symmetry plane ( $\sigma / \sigma$ pattern). Obviously, the two segments are mirror images of each other, i.e., they are heterochiral.
$\boldsymbol{C}_{w}$ Groups. Generalization of La Coupe du Roi. Taking into account the symmetry relationships shown in Table I, it is easy to deduce the results of the different dissection patterns on a general molecule of symmetry $C_{n v}$ (Table II). It is noteworthy that only molecules with an odd symmetry axis can be decomposed into heterochiral halves. Notice, however, that the fragments produced through $\sigma_{v} / \sigma_{v}$ and $C_{n} / \sigma_{v}$ strategies belong to the $C_{s}$ point group and can be further fragmented into heterochiral segments. In the last case, one could refer to the whole process as a $2 C_{n} / \sigma_{v}$ dissection pattern ( 7 , segments represented by white and shaded circles are mirror images of each other), since two sets of $C_{n}$-related bonds are disconnected. This strategy produces $2 n$ segments which are pairwise heterochiral.

It is interesting to apply our analysis to the particular case of the linear point groups, using as an example an idealized apple ( $C_{\infty v}$ point group). La coupe du roi (Figure 2a) is just a fragmentation pattern that produces two homochiral apple pieces. In order to achieve this, we need to separate two fragments related by a rotation $C_{2}$, while simultaneously destroying the symmetry planes (achieved through the horizontal cut) in what could be formally described as a $C_{2} / g$ dissection. With this in mind, we can generalize la coupe du roi by replacing the $C_{2} / \mathrm{g}$ by a $C_{n} / \mathrm{g}$ strategy: Any number of homochiral fragments of an apple can be generated by means of two sets of vertical $C_{n}$ cuts performed on the upper and lower part of the apple, respectively. The cuts on the same half of the apple must be separated by an angle of $2 \pi / n$ (where $n$ is the number of fragments to be generated), and the upper and lower cuts must be displaced by an angle $\beta$ in the range $0<\beta<2 \pi / n$ (Figure 2b). Perhaps this technique should be called la coupe du parlement. ${ }^{13}$


Unfortunately, there are no molecular apples. Any molecule belonging to the $C_{\infty \nu}$ or $D_{\infty h}$ point groups must have all of its atoms on the symmetry axis and cannot be split into isometric segments related by one of the $C_{\infty}$ or $\sigma_{v}$ operations unless we trade chemistry for nuclear physics. Isometric fragmentation of a linear molecule through $\sigma_{h}$ (or $C_{2}$ ) would result in achiral $C_{\infty v}$ segments. We can therefore conclude that linear molecules cannot produce chiral isometric segments.

Conversely, one can ask whether an apple could be cut into heterochiral parts. The $C_{\infty v}$ point group is just a particular case of $C_{n v}$ with $n=\infty$. There are two ways in which a $C_{n v}$ object can produce heterochiral segments (Table II). In one case, a $\sigma / \sigma$ cut ( $n$ odd) can yield heterochiral halves because of the absence of a perpendicular symmetry plane. This route is not operative since in $C_{\infty v}$ every symmetry plane is perpendicular to another one. On the other hand, to obtain heterochiral pairs through a $C_{2 n} / \sigma_{v}$ strategy, an infinite number of cuts must be applied. Hence an apple cannot be dissected into heterochiral segments, as previously found by Anet et al. ${ }^{3}$ Other fruits belonging to $C_{m}$ point groups with odd $n$ can be split in two heterochiral halves through a $\sigma / \sigma$ cut (an example might be an orange with an odd number of segments).
$C_{n h}$ Groups. These point groups can be obtained as a product of the corresponding $C_{n}$ group and a perpendicular symmetry plane $\sigma_{h}$. In contrast with the $C_{m v}$ groups, the proper rotations and a perpendicular symmetry plane are independent, as discussed above. As a consequence, the main results which arise for different fragmentation patterns are as follows (Table II): (i) $\sigma / \sigma$ cuts produce two heterochiral segments, each having $C_{n}$ as a symmetry operation ( $C_{n}$ point group); (ii) $C_{n} / g$ dissections yield $n$ achiral segments which retain the symmetry plane ( $C_{s}$ point group); and (iii) a $\boldsymbol{C}_{n} / \boldsymbol{C}_{n}$ dissection is only possible for $\boldsymbol{C}_{2}$ rotations. For any other $C_{n}$, there are no bonds across the symmetry axis.

Thus, it is clear that molecules belonging to $C_{n h}$ point groups cannot be fragmented into homochiral segments only. All of this can be illustrated through the example of tetrachlorocyclobutane proposed by Anet et al. ${ }^{3}$ (Figure 3a). This molecule belongs to the point group $C_{2 h}$. A $C_{2} / C_{2}$ cut (Figure 3 b ) results in achiral segments according to the above rules (point group $C_{s}$ ). On the other hand, if the molecule is cut through the symmetry plane $\sigma_{h}\left(\sigma_{h} / \sigma_{h}\right.$ cut, Figure 3 c ), heterochiral segments (point group $C_{2}$ ) are obtained.

[^2]

Figure 2. Technique for the dissection of a $C_{\infty v}$ object into two homochiral halves (la coupe du roi, a) and for its dissection into $n$ homochiral pieces (la coupe du parlement ${ }^{13}$, b).

a

b

c
Figure 3. Two dissection patterns for tetrachlorocyclobutane (a), a molecule of $C_{2 h}$ symmetry: $C_{2} / C_{2}$ (b) and $\sigma / \sigma$ (c).


Figure 4. Schematic representation and dissection patterns for [(OC)-$\left.\operatorname{Pd}(\mu-\mathrm{NC}) \mathrm{Mn}\left(\eta-\mathrm{Cp}^{\prime}\right)(\mathrm{CO})_{2}\right]$.
$S_{n}$ Point Groups. These are cyclic groups generated by the powers of improper rotations $S_{n}$, where $n$ is even, and they possess no symmetry planes. Several segmentation choices exist for such point groups according to the above analysis of the symmetry of cuts when an improper rotation is present (see Table I): (i) When an $S_{n} / \mathbf{c}$ cut is applied, two reflection-related segments result. They still possess a proper rotation $C_{n / 2}$ and are consequently heterochiral. (ii) A $C_{n / m} / \mathrm{g}$ cut yields $n / m$ segments related through $C_{n / m}$, while simultaneously destroying the $S_{n}$ operations. The segments belong to point group $C_{1}$ and are homochiral. (iii) The combined action of the two strategies is equivalent to an $S_{n} / \mathbf{g}$ cut (Table II).
Even if there is no clear-cut definition of which bonds are in a ge position and which are in a $\mathbf{g}$ position, the $S_{n} / \mathbf{g}$ and $S_{n} / \mathrm{gc}$ dissection patterns can be clearly differentiated because the first one results in $n$ segments and the latter always produces two.
An illustrative case of an $S_{n}$ molecule is provided by [(OC)-$\left.\operatorname{Pd}(\mu-\mathrm{NC}) \mathrm{Mn}\left(\eta-\mathrm{Cp}^{\prime}\right)(\mathrm{CO})_{2}\right]$, a tetranuclear cluster recently re-
ported by Braunstein et al., ${ }^{14}$ which belongs to the $S_{4}$ point group. This compound, schematically represented in Figure 4, can be dissected through an $\boldsymbol{S}_{4} / \mathrm{gc}$ cut, producing two heterochiral segments (point group $C_{2}$ ). Further disconnection via a $C_{2} / C_{2}$ cut splits each fragment into two homochiral halves. The net result, a set of $n$ pairwise heterochiral segments, could be obtained directly through an $S_{n} / \mathbf{g}$ dissection of the starting molecule.
$\boldsymbol{D}_{n d}$ Point Groups. These groups can be generated by adding a $\sigma_{v}$ reflection to a $D_{n}$ group. As a $\sigma / \sigma$ cut destroys all rotations around coplanar axes, the resulting segments retain only the perpendicular symmetry plane (which exists only for $n$ even), they belong to the $C_{s}$ point group, and they are therefore achiral. For $n$ odd, on the other hand, there are no perpendicular symmetry planes, but there is a perpendicular $C_{2}$ axis; the $\sigma / \sigma$ pattern produces heterochiral segments of $C_{2}$ symmetry. Stereographic views of such dissection patterns are presented in 8 (for $n$ even) and 9 ( $n$ odd), where the white and shaded regions represent the parts of the molecule lying above and below the plane of the paper, respectively. Of course, this strategy can only be applied when there are no atoms sitting on the $\sigma_{d}$ symmetry plane.


8
$C_{n} / C_{2}$ cuts always preserve a perpendicular $C_{2}$ axis (see 8 and 9), but all of the symmetry planes are destroyed since they are not coplanar with the binary axes. Thus, $n$ homochiral segments of $C_{2}$ symmetry are produced. If bonds at general positions are disconnected ( $\boldsymbol{C}_{n} / \mathbf{g}$ cut), all symmetry elements are destroyed and $n$ asymmetric homochiral segments result.

The $D_{n d}$ point groups can also be generated by $S_{2 n}$ and perpendicular $C_{2}$ rotations. Since we have seen that $S_{2 n} / \mathbf{p c}$ cuts can be imagined which preserve the proper rotation $C_{n}$, it is clear that segments with $D_{n}, C_{n}$, or $C_{2}$ symmetries can, in principle, be generated. $S_{2 n} / \sigma \mathrm{c}$ dissection yields two heterochiral segments of $D_{n}$ symmetry, as shown in 7 and 8 , and further disconnection ( $S_{2 n} / \sigma$ pattern) yields $2 n$ segments of $C_{2}$ symmetry which are pairwise heterochiral. Other choices can be seen in 7 and 8 and are summarized in Table II.

Finally, one could choose to cut the molecule into two pieces related by the $C_{2}$ rotations, dissecting bonds perpendicular to either the $C_{n}$ or another $C_{2}$ axis. In the former case, the result is different for the odd and even groups: a $C_{2} / C_{n}$ dissection yields two homochiral segments of $C_{2}$ symmetry when $n$ is even, but two
(14) Braunstein, P.; Oswald, B.; Tiripicchio, A.; Tiripicchio-Camellini, M. Angew. Chem., Inl. Ed. Engl. 1990, 29, 1140.

achiral $C_{s}$ segments when $n$ is odd. The result of a $C_{2} / C_{2}$ dissection is presented in Table II.
An example of a $D_{2 d}$ molecule is provided by bisnoradamantane ${ }^{15}$ (10). Despite the large number of dissection

patterns available for $D_{n d}$ molecules, most of them cannot be applied to this molecule: $\sigma_{d} / \sigma_{d}, C_{n} / C_{2}, \boldsymbol{S}_{2 n} / \sigma c, S_{2 n} / \sigma, S_{2 n} / C_{2}$, and $\sigma_{d}$ patterns are forbidden because there are atoms sitting on the corresponding symmetry elements. $C_{n} / \mathrm{g}$ and $C_{2} / C_{n}$ patterns do not disconnect this molecule. Thus, we are left with only $\boldsymbol{S}_{2 n} / \mathbf{g c}$ and $\boldsymbol{S}_{2 n} / \mathrm{g}$ strategies to cut this molecule in isometric segments. In the $\boldsymbol{S}_{2 n} / \mathrm{gc}$ pathway, we cut a bond in a general position (indicated by an arrow in 10) and all of the equivalent bonds related through $S_{4}$ rotations. The result is two heterochiral segments of $C_{2}$ symmetry (Table II), which could be further disconnected to yield four pairwise heterochiral asymmetric fragments.

[^3]

Figure 5. Hierarchical relationship of the 22 subgroups of the icosahedral point group $I_{h}$ (adapted from ref 17).

It is interesting to compare the case of bisnoradamantane with the closely related molecule of twistane (11). Despite the similarity of the two molecules, twistane ( $D_{2 d}$ point group) can only be segmented into homochiral pieces, and a convergent synthesis of such a molecule is not known. ${ }^{16}$


11
Point Groups with Higher Symmetry. For molecules belonging to point groups of high symmetry other than those discussed above, the suppression of one symmetry element is not enough to yield disymmetric segments. As an example, the symmetry point groups of the fragments obtained through different dissection patterns from a $D_{n h}$ molecule are shown in Table II; in all cases the segments are achiral. The symmetry therefore must be previously reduced, e.g., by chemical modifications, and then the appropriate fragmentation pattern chosen to produce either homo- or heterochiral segments.

An example of a molecule with high symmetry is provided by dodecahedrane. This molecule belongs to the icosahedral point group, $I_{h}$, and no simple fragmentation into chiral isometric segments is available for dodecahedrane. Through chemical modifications, however, its symmetry can be lowered. A scheme of the hierarchical relationships of the 22 subgroups of $I_{h}$ is shown in Figure $5,{ }^{17}$ where the point groups corresponding to derivatives which can be cut into heterochiral segments, according to the above analysis, are enclosed in thick boxes. The shaded boxes correspond to phantom point groups, ${ }^{18}$ i.e., those point groups for which no derivative of dodecahedrane can exist.

In accordance with these relationships, one can gradually lower the symmetry, e.g., from $I_{h}$ to $D_{3 d}$, to $C_{2 h}$, and to $C_{i}$ (heterochiral segments) or $C_{2}$ (which can generate only homochiral segments), as shown in Figure 6. Notice that the $C_{2}$ and $C_{i}$ isomers are built up from the same segments, but both enantiomers of the segment are needed to form the $C_{i}$ isomer, whereas two segments of an optically pure building block give one enantiomer of the $C_{2}$ isomer. Hence, a racemate of the fragments can produce a mixture of the $C_{i}$ plus a racemate of the $C_{2}$ isomers, but optically pure fragments produce only the corresponding $C_{2}$ enantiomer (also optically pure).

A different approach consists of lowering the symmetry from $I_{h}$ to $D_{3 d}$ (the approach proposed by Müller, Woodward, and Jacobsen, independently, for the synthesis of dodecahedrane from

[^4]

Figure 6. Symmetry lowering and dissection patterns for dodecahedrane.
two moieties of the achiral triquinacene ${ }^{19}$ ), and then to $S_{6}$ (the approach proposed by Serratosa and co-workers ${ }^{8}$ using two heterochiral segments as building blocks), also shown in Figure 6. The reader can use the relationships of Figure 5 and the results in Table II to design new segmentation patterns.

A related case is that of footballane, the $\mathrm{C}_{60}$ molecule with $I_{h}$ symmetry. One can homolytically split such a molecule ${ }^{20}$ in two halves of $C_{5 v}$ symmetry, but first one must single out the bonds which are going to be disconnected, therefore lowering the symmetry from $I_{h}$ to $D_{5 d}$ (see Figure 5). If the disconnection is heterolytic, some asymmetry must be introduced in the disconnected bonds, therefore lowering the symmetry of the molecule to $D_{5}$ and producing homochiral segments of $C_{5}$ symmetry. ${ }^{21}$

## Conclusions

From the above discussion and the results in Table II, a first hint of the ways in which a particular molecule can be fragmented into isometric segments, as well as their relative chiralities, can be obtained if the symmetry point group of the molecule is known. We can still try to place the results of Table II in a more general context and find the relationship between a molecule, be it chiral or achiral, and its isometric segments. The following ruies can be deduced.
(1) Chiral molecules can only be fragmented into homochiral isometric segments. Conversely, for the convergent synthesis of an optically resolved chiral molecule, optically pure chiral segments must be used. The use of racemic segments would result in a racemate of the target molecule. Furthermore, heterochiral segments can only produce achiral molecules.
(2) In general, isometric dissection of achiral molecules results in pairs of heterochiral segments, with a few exceptions discussed below. This means that the use of a racemic mixture for the convergent synthesis of achiral molecules is a good strategy.
(3) Achiral molecules of symmetry $C_{n v}$ or $D_{n d}$ can be dissected into homochiral segments through a $C_{n} / \mathbf{g}$ ( $C_{m}$ or $D_{n d}$ point groups) or a $C_{n} / C_{2}$ ( $D_{n d}$ point group) dissection pattern. These are the

[^5]only cases in which homochiral segments can be assembled into achiral molecules and constitute a generalization of la coupe du roi, generally used for $C_{n v}$ molecules only.

The first conclusion may have some relevance to the fact that living beings prefer homochirality, i.e., they use only the L series of amino acids in proteins and only the $D$ family of nucleotides in nucleic acids, a fact closely related to the origin of life. ${ }^{22.23}$ Since chain compounds can be regarded as cyclic systems with an infinite number of members, ${ }^{24}$ our symmetry analysis above indicates that,

[^6]in proteins or nucleic acids, an enantiomeric chain compound can only be obtained from homochiral building blocks.

Acknowledgment. The authors are indebted to P. Alemany, J. J. Novoa, and P. Braunstein for enlightening discussions, to R. Rycroft for carefully reading the manuscript, and to F. Vilardell for part of the drawings. Financial support from DGICYT (Grant No. PB89-0268) is gratefully acknowledged.

Supplementary Material Available: Drawings of 35 fragmentation patterns for 23 molecules ( 9 pages). Ordering information is given on any current masthead page.
(24) See: Gerstein, B. C. J. Chem. Educ. 1973, 50, 316.

# On the Photodecomposition Mechanism of $o$-Diazonaphthoquinones 

Mónica Barra, ${ }^{1}$ T. A. Fisher, ${ }^{2}$ G. J. Cernigliaro, ${ }^{2}$ R. Sinta, ${ }^{*, 2}$ and J. C. Scaiano*,1,3<br>Contribution from the Department of Chemistry, University of Ottawa, Ottawa, Canada KIN 6 N5, Shipley Company, Inc., 455 Forest Street, Marlboro, Massachusetts 01752, and Steacie Institute for Molecular Sciences, National Research Council, Ottawa, Canada K1A OR6. Received July 2, 1991


#### Abstract

The mechanism for the photodecomposition of several o-diazonaphthoquinones has been examined in acetonitrile solution using time-resolved laser flash photolysis techniques. It is concluded that the Wolff rearrangement, which involves the formation of a ketene intermediate, can be regarded as a concerted process in the nanosecond time scale. It is suggested that the reaction of the ketene with water, which is well known to yield 3 -indenecarboxylic acids, involves the intermediacy of a ketene hydrate. Pyridine, a molecule frequently employed as a carbene trap/probe, efficiently traps the ketene in these systems; this scavenging reaction can be employed as a probe for the study of the dynamics of ketene reactions, but in some systems it may represent a problem in carbene studies if the possibility of ketene reactions is not considered.


## Introduction

The phototransformation of 2-diazo-1,2-naphthoquinones (DNQs) into the corresponding 3-indenecarboxylic acids (3-ICAs) (eq 1) via the Wolff rearrangement has been widely studied and has numerous applications in photoresist technology. ${ }^{4}$


It is well known that the photodecomposition of DNQs produces an intermediate ketene, which upon reaction with water yields the corresponding 3-ICA. It has been suggested that in some cases a long-lived intermediate ketene (the transient decay time is of the order of seconds) can absorb another photon, leading to unwanted photochemistry, which in the photoresist field is usually referred to as a reciprocity failure. ${ }^{5}$

The conversion of $o$-diazo ketones into ketenes involves a 1,2 migration of a carbon atom, which is known as the Wolff rearrangement. Despite many investigations, the mechanism involved in this process is still being debated. The focus of the discussion is whether the loss of nitrogen and the 1,2 migration of the carbon

[^7]Scheme I

atom occur in a concerted manner or the Wolff rearrangement is a two-step reaction which involves an $\alpha$-keto carbene and/or an oxirene-like intermediate, as represented in Scheme I. On the basis of the studies already reported, one must point out that the mechanism will depend on the specific type of o-diazo ketone being studied. ${ }^{6}$

The mechanism for the photoconversion of DNQs into 3-ICAs in solution is a matter of some discussion and controversy. There have been different results on the number, sequence, and spectroscopic properties of the intermediates formed, such as the ketene. ${ }^{7-12}$
(6) Fenwick, J.; Frater, G.; Ogi, K.; Strausz, O. P. J. Am. Chem. Soc. 1973, 95, 124.
(7) Nakamura, K.; Udagawa, S.; Honda, K. Chem. Letl. 1972, 763.
(8) Delaire, J. A.; Faure, J.; Hassine-Renou, F.; Soreau, M. New J. Chem. 1987, 11, 15.
(9) Tanigaki, K.; Ebbesen, T. W. J. Am. Chem. Soc. 1987, 109, 5883.
(10) Tanigaki, K.; Ebbesen, T. W. J. Phys. Chem. 1989, $93,4531$.


[^0]:    (1) Corey, E. J. Q. Rev. Chem. Soc. 1971, 25, 455; Chem. Soc. Rev. 1988, 17, 111 .
    (2) Two molecules are isometric if their labeled graphs are the same, i.e., if the atoms and their connectivity (bonds) are the same. See ref 3 and references therein.
    (3) Anet, F. A. L.; Miura, S. S.; Siegel, J.; Mislow, K. J. Am. Chem. Soc. 1983, $105,1419$.
    (4) Velluz, L.; Valls, J.; Mathieu, J. Angew. Chem., Int. Ed. Engl. 1967, 6, 778. Bertz, S. H. J. Chem. Soc., Chem. Commun. 1984, 218.
    (5) Cinquini, M.; Cozzi, F.; Sannicolò, F.; Sironi, A. J. Am. Chem. Soc. 1988, $110,4363$.
    (6) "Narcissistic, from Narkissos, youth who fell in love with his reflection in water", The Oxford English Dictionary [cf. L. A. Salem, J. Durup, G. Bergeron, D. Cazes, X. Chapuisat, H. Kagan (J. Am. Chem. Soc. 1970, 92 , 4472), "a reaction is defined as narcissistic if reactant(s) and product(s) are mirror images with respect to a fixed plane and if the image of the reactant(s) undergoes the reverse 'reaction' to the image of the product(s)"].
    (7) Bertz, S. H. J. Am. Chem. Soc. 1982, 104, 5801.
    (8) Carceller, E.; Garcia, M. L.; Moyano, A.; Pericàs, M. A.; Serratosa, F. Tetrahedron 1986, 42, 1831.
    (9) Cotton, F. A. Chemical' Applications of Group Theory, 3rd ed; J. Wiley: New York, 1990.

[^1]:    (10) Lehn, J. M.; Rigault, A.; Siegel, J.; Harrowfield, J.; Chevrier, B.; Moras, D. Proc. Natl. Acad. Sci. USA 1987, 84, 2565.

[^2]:    (13) As the general way to cut an apple into any number of homochiral slices describes a more advanced technique than the partition into two pieces known as la coupe du roi, we propose a name which assumes parliamentary democracy as a higher degree of social organization than monarchy.

[^3]:    (15) Freeman, P. K.; Rao, V. N. M.; Bigam, G. E. J. Chem. Soc., Chem. Commun. 1965, 511 . Vogt, B. R.; Sutter, S. R.; Hoover, J. R. E. Tetrahedron Lett. 1968, 1609.

[^4]:    (16) Serratosa, F. Organic Chemistry in Aclion; Elsevier: Amsterdam, 1990; pp 283-297.
    (17) Salthouse, J. A.; Ware, M. J. Point Group Character Tables and Related Data; Cambridge University Press: Cambridge, 1972.
    (18) Brocas, J. J. Am. Chem. Soc. 1986, 108, 1135.

[^5]:    (19) Müller, D. M. Chem. Weekbl. 1963, 59, 334. Woodward, R. B.; Fukunaga, T.; Kelly, R. C. J. Am. Chem. Soc. 1964, 86, 3162. Jacobson, I. T. Acta Chem. Scand. 1967, 21, 2235. See also: Roberts, W. P.; Shoham, G. Tetrahedron Lett. 1981, 4895.
    (20) McKee, M. L.; Herndon, W. C. THEOCHEM 1987, $38,75$.
    (21) For other segmentation patterns of footballane, see: Fabre, C.; Rassat, A. Comp. Rend. Acad. Sci. Paris, Ser. II 1989, 308, 1223 and references therein.

[^6]:    (22) Brack, A. In La Symétrie Aujourd'hui; Éditions du Seuil: Paris, 1989.
    (23) Hargittai, I.; Hargittai, M. Symmetry through the Eyes of a Chemist; VCH Publishers: New York, 1987; p 60.

[^7]:    (1) University of Ottawa.
    (2) Shipley Co., Inc.
    (3) National Research Council.
    (4) Reiser, A. Photoreactive Polymers: The Science and Technology of Resists; John Wiley and Sons: New York, 1989; pp 409.
    (5) Sheats, J. R. IEEE Trans. Elec. Dev. 1988, ED-35, 129.

